

# MATH 551 - Problem Set 7

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## 1.

- a) If  $ABC\Delta$  and  $A'B'C'\Delta$  are perspective with respect to point  $P$  with  $L = BC \cap B'C'$ ,  $M = CA \cap C'A'$  and  $AB \parallel A'B'$ , then  $LM \parallel AB \parallel A'B'$ .
- b) Given  $A'B'C'\Delta$  perspective with respect to point  $P$ , and point  $C$  on line  $PC'$  and point  $B$  on line  $PB'$ . Let  $c$  be the line containing  $C$  parallel to  $A'P$  and  $b$  be the containing  $B$  parallel to  $A'P$ , then we must have  $K = b \cap A'B'$ ,  $L = c \cap A'C'$ , and  $M = CB \cap C'B'$  are collinear.
- c) Given two lines, one containing  $B$  and  $B'$  and the other containing  $C$  and  $C'$ , let lines  $x \parallel y$  where  $x$  goes through point  $B$  and  $y$  goes through point  $C$  and likewise lines  $z \parallel f$  where  $z$  goes through  $B'$  and  $f$  goes through  $C'$ , then we must have that  $x \cap z$ ,  $z \cap f$ , and  $BC \cap B'C'$  are collinear.

## 2.

- a) Given  $A, B, C$  are collinear and  $A', B', C'$  are collinear, and  $B'C \parallel C'B$  and  $AB' \parallel A'B$ , then we must have that  $AC' \parallel CA'$ .
- b) Given  $A', B', C'$  collinear and line  $a$  containing  $C'$  and line  $b$  containing  $A'$ , where  $a \parallel b$  and line  $d$  containing  $B'$  and line  $c$  containing  $A'$  where  $d \parallel c$  and line  $g$  containing  $C'$  and line  $f$  containing  $B'$  where  $g \parallel f$ , we must have  $b \cap f$ ,  $d \cap a$ , and  $c \cap g$  are collinear.